M3 Challenge 2024:

A Tale of Two Crises: The Housing Shortage and Homelessness

TEAM #17868March 4th, 2024

1 Executive Summary

To the Minister Rowley,

With rapid population growth in urban centers, homelessness has become an increasingly important issue for urban planners and city designers. For example, in Manchester, homelessness has more than tripled over 14 years [6]. As housing supply continues to rapidly decrease in relation to demand and prices continue to skyrocket, more and more people will begin to have to face homelessness as their only option, putting pressure on the social welfare programs that support these impoverished people. Therefore, it is of utmost importance to develop and pass remedial legislation to allow for more affordable housing for the future.

We predicted the number of total housing units in both Manchester and Brighton & Hove over the next 10, 20, and 50 years, corresponding to the years 2031, 2041, and 2071 respectively. Using a linear regression model, we used data from 1993-2022 to extrapolate future trends about the number of total housing units in these two cities. We found that housing is only set to increase to 137,400 units in 2031, 143,400 units in 2041, and 161,500 units in 2071 in Brighton & Hove. These numbers are 254,800, 274,100, and 332,100 units respectively for Manchester. This gradual increase in housing is a step in the right direction, but needs more help fro legislators to increase the rate of building.

Next, we created two sinusoidal-trend models to predict homelessness in Brighton & Hove and Manchester. Utilizing the time series data from 2008-2022, we predicted that over the next 10, 20, and 50 years the percentage of the population that is homeless would be 0.63%, 0.56%, and 0.47% for Brighton & Hove and 0.63%, 1.81%, and 3.03% for Manchester. These models gave us the ability to model the long-term behavior of homelessness in each of the desired regions.

We then conducted a thorough analysis of the myriad of factors that may contribute to homelessness in Brighton & Hove, building a heatmap of correlation coefficients to determine which factors most closely positively or negatively correlated with homelessness. Using these key determinants of homelessness, we utilized a multiple linear regression model in order to fit the homelessness data for Brighton & Hove for 2008-2022, giving us the ability to predict these same effects on homelessness given predictions on data such as population, housing disparity, etc.

We believe these results will assist you in determining the correct path forward to begin solving this issue for England's regions.

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2 Global Assumptions

- 1. All housing, either occupied or vacant, will be considered as part of the housing supply.
 - Justification: Data is provided for both vacant and occupied housing by the Mathworks Math Modeling Challenge, and both will be treated the same way, even in our analysis of homelessness. [6]
- 2. Those who are eligible for homeless aid but are not unhoused will be neglected.
 - Justification: The data given by the Mathworks Math Modeling Challenge Data Statement provides the count of those who are homeless with priority need, those who are homeless, but without priority need, and those who are eligible, but are not homeless. [6] We will only consider the first two categories, as those are the people who are currently true homeless
- 3. COVID-19 will not affect housing supply after 2024
 - Justification: Coronavirus has slowed considerably in the UK since its peak in 2020-2021 [5], therefore our model will not consider the previous impacts of COVID-19.

4. Assumption: Zoning laws will not change drastically over the next 50 years

• Justification: One of the most significant roadblocks to new housing in the UK are zoning laws and regulations [14]. Hence, if these change, they could drastically slow down or increase production of new housing. However, for simplicity's sake, we will assume that no significant zoning laws will change over the next 50 years.

3 Q1: It Was the Best of Times

3.1 Defining the Problem

The question asks us to develop a model predicting housing supply in 2031, 2041, and 2071 in Brighton & Hove and Manchester. To this end, our model will consider past housing supply from these two regions.

3.2 Assumptions

1. Assumption: Housing supply data from 1993-2021 is sufficient to determine housing supply data over the next 50 years

• Justification: The data provided by the Mathworks Math Modeling Challenge is from 1993 to 2021 [6], so we will assume that this period of time provides sufficient data for our model

3.3 Variables

Variable	Description	Unit
S_{bh}	Total housing units in Brighton & Hove	Housing Units
S_m	Total housing units in Manchester	Housing Units
t	Time	Years

3.4 The Model

3.4.1 Developing the Model

We chose a linear regression model to predict changes in housing data over time. Linear regression models are often used to predict future trends using present/past data, and in finance and academics [7], so they can apply to the housing market. Depending on the depth and accuracy of the training data, linear regression models are generally accurate across both short and long timeframes. Our data exhibits linearity (as shown in Figure 1), so we decided a linear regression model would be optimal.

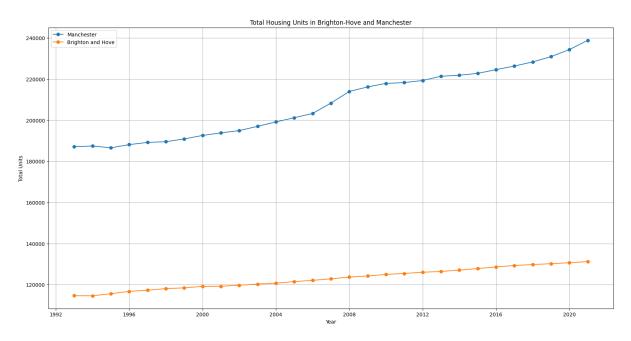


Figure 1: Housing data of Manchester (blue) and Brighton & Hove (orange) plotted over the years 1993-2021 [6].

A linear regression model develops a line of best fit that relates the variables x, y with an equation in the format y = mx + b. The coefficient m, which represents the slope of the line, and the constant b, which represents the y-intercept of the line. The values of m and b can be found with the equations below [8]:

$$m = \frac{n(\Sigma xy) - (\Sigma x)(\Sigma y)}{n(\Sigma x^2) - (\Sigma x)^2} \tag{1}$$

$$b = \frac{(\Sigma y)(\Sigma x^2) - (\Sigma x)(\Sigma x y)}{n(\Sigma x^2) - (\Sigma x)^2}$$
(2)

Where:

- x is the years.
- y is the total housing units in the given city.

An Auto-Regressive Integrated Moving Average (ARIMA) model was also tested, as it would help accommodate for the slight non-linearity of the Manchester housing data and identify any potential seasonality and cyclical behavior in the data. The governing equation of ARIMA can be found below:

$$y'_{t} = c + \phi_{1}y'_{t-1} + \dots + \phi_{p}y'_{t-p} + \theta_{1}\epsilon_{t-1} + \dots + \theta_{q}\epsilon_{t-q} + \epsilon_{t}$$

$$(3)$$

Where:

• y'_t is the differenced time series value at time t. The prime notation indicates differencing, which is used to make the series stationary.

- c is a constant term that accounts for the mean level in the series.
- ϕ_1, \ldots, ϕ_p are the coefficients of the autoregressive terms, where each term represents the impact of the *p* previous values of the time series on the current value.
- $y't 1, \ldots, y't p$ are the p previous values of the differenced time series, indicating the autoregressive component of the model, which relates the current value of the series to its past values.
- $\theta_1, \ldots, \theta_q$ are the coefficients of the moving average terms, where each term represents the impact of the q previous forecast errors on the current value.
- $\epsilon_{t-1} \ldots, \epsilon_{t-q}$ are the q previous forecast errors. These errors are the differences between the past actual values and the past predicted values, indicating the moving average component of the model.
- ϵ_t is the error term at time t, representing the randomness or unpredictability in the series at time t. [3]

3.4.2 Executing the Model

To model the changes in housing supply, data that provided the total number of housing units available over a given time interval in each of the two regions was needed. Our team sourced the number of total housing units from the provided data statement [6]. The data provided in the data statement had the most complete and reliable data on the total number of housing units for a 30-year interval. While more data was preferable for more accurate predictions, a literature survey revealed no accessible sources that contained data as thoroughly cleaned and reviewed as that of the data statement.

After importing the data into our Jupyter notebook, we cleaned it and organized it into Pandas DataFrames. We used all of the provided data and used the *.polyfit()* function from NumPy to determine the linear regression model for each of the two regions' housing supplies. We set the *deg* parameter to one, as both city's housing unit data exhibited linearity. We then applied the linear regression model to predict the changes in housing supply by 2031, 2041, and 2071 (10, 20, and 50 years into the future from the most recent measurement year).

3.5 Results

The linear regression model we chose accounts for the lack of data and linear nature of the data provided. The deviations from the linear model in the Manchester housing data are very slight and are eventually balanced by deviations in the opposite direction, while there are no significant deviations from the linear model in the Brighton and Hove housing data. The results of the fit of the data provided by the model are seen in Figure 2.

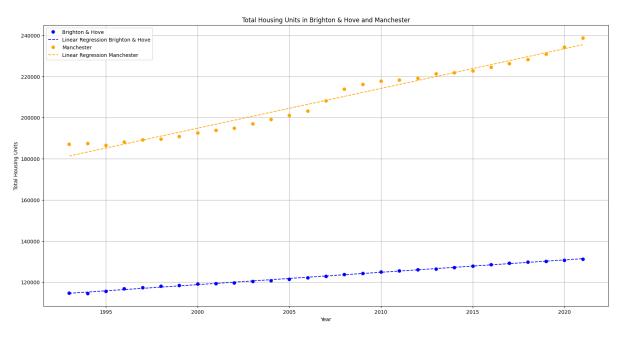


Figure 2: Line of best fit as predicted by linear regression model on housing data.

Next, the linear regression model was applied to future time frames (2031, 2041, and 2071 for 10, 20, and 50 years in the future, respectively). The predictions are shown in Figure 3.

The predictions were graphed with confidence intervals to ensuring that the model was reliable for making predictions. The narrow confidence interval suggests that a model has a tighter fit to the data, leading to more precise predictions. Moreover, the linear regression model had an $R^2 = 0.997$ for the Brighton & Hove housing data and an $R^2 = 0.974$ for the Manchester housing data, suggesting a tight fit to the given data. The future predictions with confidence intervals are seen in Figure 3

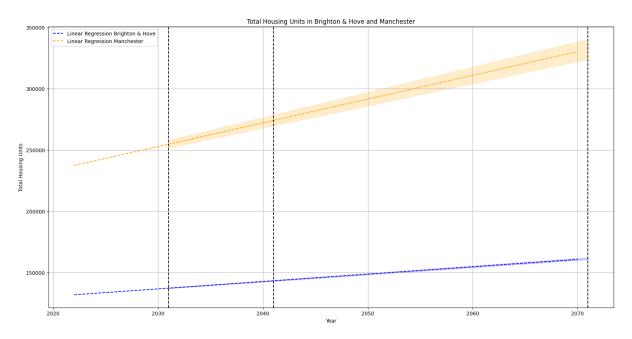


Figure 3: Predicted total housing units in Brighton & Hove and Manchester in 2031, 2041, and 2071. Confidence intervals are plotted in areas where predictions are made.

Year	Predicted Low	Predicted High	
2031	$137,\!100$	137,400	137,700
2041	143,000	143,400	143,900
2071	160,700	161,500	162,300

Table 1: Results for Brighton & Hove * Values are rounded to 4 sig-figs

Year	Predicted Low	Predicted Average	Predicted High		
2031	251,600	254,800	258,000		
2041	269,700	274,100	278,500		
2071	324,000	332,100	340,200		

 Table 2: Results for Manchester

The ARIMA model that was tested failed to properly model the data, as the volume of the data was insufficient to form a foundation upon which ARIMA could make predictions. Thus, the ARIMA model's predictions were linear in shape as well, but fit the data less accurately than the linear regression, as seen in Figure 4.

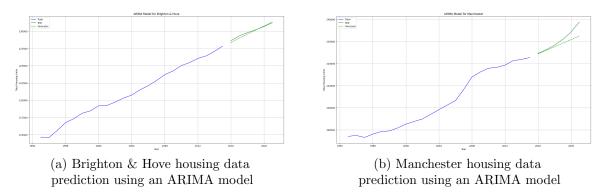


Figure 4: Testing an ARIMA Model

3.6 Discussion

In summary, our model predicts that there will be around 161,500 total housing units in Brighton & Hove and around 332,100 total housing units in Manchester by 2071. Hence, we can conclude that the number of total housing units in both regions will gradually grow, with Manchester's count increasing faster than than Brighton & Hove's.

3.7 Sensitivity Analysis

We performed a sensitivity analysis on our linear regression model by adjusting it's intercept and slope by the intervals seen below. The highest error was found only when adjusting the slope up to 1.05 while also adjusting the intercept down to 95% of its original value, or vice versa. When both the slope and intercept are adjusted in the same direction, the error is extremely low, only reaching a high of 5%.

	Error in Intercept								
Error in Slope	0.95			1			1.05		
	2031	2041	2071	2031	2041	2071	2031	2041	2050
0.95	-5.0	-5.0	-5.0	-44.4	-42.8	-38.5	-83.8	-80.5	-72.1
0.975	17.2	16.4	14.3	-22.2	-21.4	-19.3	-61.6	-59.1	-52.8
1	39.4	37.8	33.5	0.0	0.0	0.0	-39.4	-37.8	-33.5
1.025	61.6	59.1	52.8	22.2	21.4	19.3	-17.2	-16.4	-14.3
1.05	83.8	80.5	72.1	44.4	42.8	38.5	5.0	5.0	5.0

Table 3: Sensitivity Analysis of Slope and Intercept for Brighton &Hove Linear Regression

	Error in Intercept								
Error in Slope	0.95			1			1.05		
	2031	2041	2071	2031	2041	2071	2031	2041	2071
0.95	-5.0	-5.0	-5.0	-77.0	-71.9	-60.3	-149.1	-138.9	-115.5
0.975	33.5	31.0	25.1	-38.5	-36.0	-30.1	-110.5	-102.9	-85.4
1	72.0	66.9	55.3	0.0	0.0	0.0	-72.0	-66.9	-55.3
1.025	110.5	102.9	85.4	38.5	36.0	30.1	-33.5	-31.0	-25.1
1.05	149.1	138.9	115.5	77.0	71.9	60.3	5.0	5.0	5.0

Table 4: Sensitivity Analysis of Slope and Intercept for ManchesterLinear Regression

Therefore, our model can be considered a reasonable predictor of total housing units in these two regions, but cannot guarantee predictions for new housing.

3.8 Strengths and Weaknesses

The linear regression model is the strongest model for the data given. The data for total housing units for both Brighton & Hove and Manchester both display a visually linear correlation over time, which allows for the linear regression model to excel at predicting future values. Other models that may have fit the model more appropriately, such as ARIMA, could not offer accurate predictions due to a lack of volume of data.

However, there are some weaknesses to the linear regression approach to the problem. It is possible that the subtler trends in the data, like seasonality and cyclical behavior, were overlooked by the linear regression model, thus "smoothing over" potentially important details for future predictions. ARIMA and other generalized models potentially could account for these factors if given more in-depth data.

4 Q2: It Was the Worst of Times

4.1 Defining the Problem

The question requires developing a model that can predict the homeless population in 2032, 2042, and 2072 in Brighton & Hove and Manchester. The model must consider the past homeless population from these two region to forecast the future homeless population.

4.2 Assumptions

1. The population growths of Manchester and Brighton & Hove are logistic

• Justification: The population of any general region can be modeled with an exponential function that plateaus at the region's carrying capacity, the contributors to which are multivariate, thus following the logistic growth model [13]. It is assumed that Manchester and Brighton & Hove follow the pattern observed in many other places.

2. Assumption: Homelessness data from the past is sufficient to determine future trends about homelessness

• Justification: The data provided by the Mathworks Math Modeling Challenge is only from 2008 to 2022, so we will assume that this data is not an outlier and is representative of the future trends.

3. No major legislative change will take place

• Justification: The homeless issue in the UK, including Manchester and Brighton & Hove, is reaching crisis levels [9], so remedial legislation should and will most likely be passed. This will likely mean that homelessness never reaches the levels that any extrapolation from the present will predict, but since we cannot determine the effect of this potential future legislation, we must neglect this possibility.

Variable	Description	Unit
U_{bh}	Total homeless households in Brighton & Hove	Households
U_m	Total homeless household in Manchester	Households
P_{bh}	Total households in Brighton & Hove	Households
P_m	Total households in Manchester	Households
$U_{bh\%}$	Percent of households in Brighton & Hove that are homeless	%
$U_{m\%}$	Percent of households in Manchester that are homeless	%
t	Time	Years

4.3 Variables

4.4 The Model

4.4.1 Developing the Model

To predict homelessness in the regions of Brighton & Hove and Manchester for up to 50 years in the future, we developed two separate models that were tailored to the conditions of each city. For Brighton & Hove, we developed a sinusoidal regression fit, while for Manchester, we developed a sinusoidal fit with a trend.

Sinusoidal regression creates a curve of best fit that fits cyclical data with a sine function as shown in Equation 4. To extend this model further, a linear trend can be added as shown in Equation 5.

$$U_{bh\%} = \gamma \sin(\zeta t + \phi) + \beta + \epsilon \tag{4}$$

$$U_{m_{\text{ex}}} = \alpha * x + \gamma \sin(\zeta t + \phi) + \beta + \epsilon \tag{5}$$

(6)

where:

- α is the slope of the linear trend component.
- γ is the amplitude of the sinusoidal curve.
- ζ is the period of the sinusoidal curve.
- ϕ is the phase shift of the sinusoidal curve.
- β is the vertical shift of the sinusoidal curve.
- ϵ is the residual error. [2]

We also tested a correlation between an affordability score, which was calculated by dividing the median house sales price by inflation-adjusted median salary, and homelessness. However, this linear regression proved insignificant, as there was no correlation for Brighton & Hove, and the positive correlation determined for Manchester was notably weak, registering an R^2 coefficient of only 0.70.

Furthermore, we tested a correlation between the disparity between housing availability and overall population and homelessness in the two regions. However, for both regions, the correlation was weak at best, with an R^2 coefficient of 0.61 for Manchester.

We also tested a variety of models using the PyCaret AutoML library to fit multiple models to the data through machine learning.

4.4.2 Executing the Model

The data statement provided by the Mathworks Math Modeling Challenge [6] was used as the primary source of the data used for the model, as the other sources found did not have as extensive of a time range and as clean data for homelessness, total population, housing prices, and total housing unit count in the two regions as the data statement. This dataset did include some missing data; hence we linearly interpolated the value from the values around it in order to replace it.

To fit a sinusoidal curve to our data, we used the .curve_fit() function from the SciPy library. The function uses gradient descent as an optimizer and non-linear least squares as a loss function to find the curve of best fit in the form of any generalized function.

To add a trend to the sinusoidal fit, we combined the sinusoidal regression model used for the Brighton & Hove homelessness data and the linear regression model used for predicting future housing supply in Q1. By combining these, the sinusoidal fit followed an upward trend that better fit the data.

4.5 Results

Below is the table for our predictions of the percent of the population that will be homeless at 2032, 2042, and 2072. For reference, the last given data point from 2022 for the percentage of population facing homelessness was 0.53% and 0.17% for Manchester and Brighton & Hove, respectively.

Year	Homeless Percent of Population					
Teal	Brighton & Hove (%)	Manchester (%)				
2032	0.63	0.63				
2042	0.56	1.81				
2072	0.47	3.03				

Table 5: Predicted Homeless Percentage of Population for Brighton &Hove and Manchester

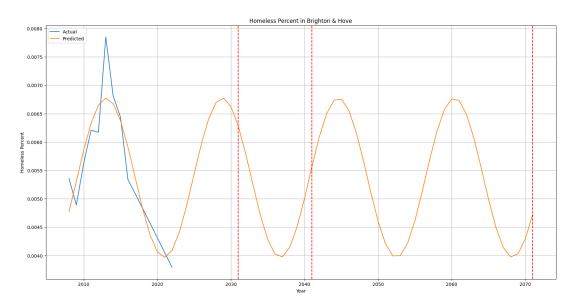


Figure 5: Extrapolating Sinusoidal Model to predict change in Homelessness in Brighton & Hove for the next 10, 20, and 50 years

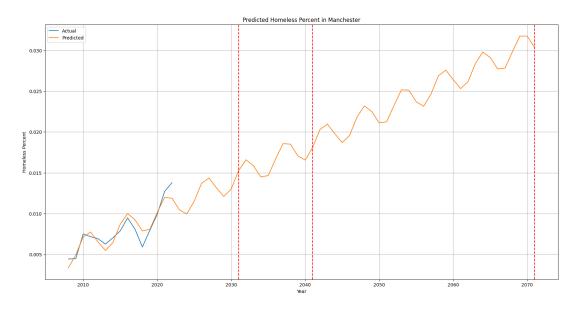


Figure 6: Extrapolating Sinusoidal Curve with Trend Model to predict change in Homelessness in Manchester for next 10, 20, and 50 years

4.6 Discussion

In summary, our model predicts that 0.63%, 0.56%, and 0.47% of the total population of Brighton & Hove will be homeless in 2032, 2042, and 2072, respectively. For Manchester, our model predicts that 0.63%, 1.81%, 3.03% of the total population will be homeless at the same time intervals. From this, we can conclude that if no remedial legislation is passed, homelessness will quickly become an unmanageable runaway issue in Manchester, and will linger as an economic and quality-of-life hamper in Brighton & Hove.

4.7 Strengths and Weaknesses

Both of our models' strengths lie in their specificity, as they focus only on the data of one city, rather than a general trend across both cities that would be less accurate to either. The models also focus specifically on the homelessness, rather than using correlations between other variables and homelessness, which could introduce confounding variables or interpret correlation as causation.

However, the lack of data could lead to issues in generalizability and overfitting. Considering the missing data in the Brighton & Hove set, it is possible that the trend fitted by the model would not truly extrapolate into the future.

5 Q3: Rising from the Abyss

5.1 Defining the Problem

The question asks us to develop a model that can predict the effects of unforeseen circumstances like economic recessions, or increased migrant populations to help a city determine a long-term plan and thus address homelessness. We assessed a myriad of different factors that contribute to homelessness to address the effects of these circumstances.

5.2 Assumptions

1. Assumption: Predictions can be made from the past data available.

• Justification: The data provided by the Mathworks Math Modelling Challenge is only from 2018 to 2022, so we will assume for sake of simplicity that this time frame provides sufficient data for our model.

2. Assumption: All variables will have an effect on the homeless population in Brighton & Hove.

• Justification: Most of the data provided in the data statement is related to income, housing availability, or population, which all can have an impact on the ability of an individual to secure a home.

Variable	Description	Unit
U_{bh}	Total homeless/unhoused households in Brighton & Hove	Households
P_{bh}	Total households in Brighton & Hove	Households
T_{bh}	Total population in Brighton & Hove	People
t	Time	Years
A_m	Median Age	Years
I_m	Median Income	Pounds
H_d	Housing Deficit/Disparity	Housing Units

5.3 Variables

5.4 The Model

5.4.1 Developing the Model

To identify the core factors impacting homelessness in a given city, we utilized a correlation heat map to determine the explained variance each factor contributed. This approach not only led to the identification of key determinants but also provided insights into the interplay between different factors. Some factors that we tested that didn't show any significant correlation to homelessness or other significant contributors included increase in population, England's total homeless population, and the average household size. As we were looking for factors that either significantly positively or negatively correlated with homelessness, signified by a value near 1 or -1, these factors did not exhibit a high enough correlation coefficient to be included at all within the multiple linear regression.

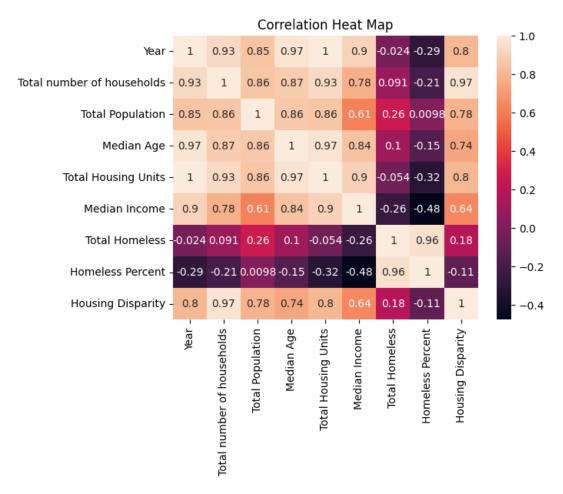


Figure 7: Heatmap of correlation between multiple factors contributing to homelessness in Brighton & Hove.

5.4.2 Executing the Model

To model the changes in homelessness, we gathered all our Brighton & Hove data for 2008-2021 from the provided data statement [6]. We utilized a multiple linear regression using the Python library SciPy. To address missing data, we decided to use linear interpolation to derive them from the surrounding points due to the minimal number of data samples.

5.5 Results

Figure 8 is the graph for our multiple regression model's fit to the homelessness data given for Brighton & Hove. As can be seen, the multiple linear regression fit is strong with an $R^2 = 0.85$.

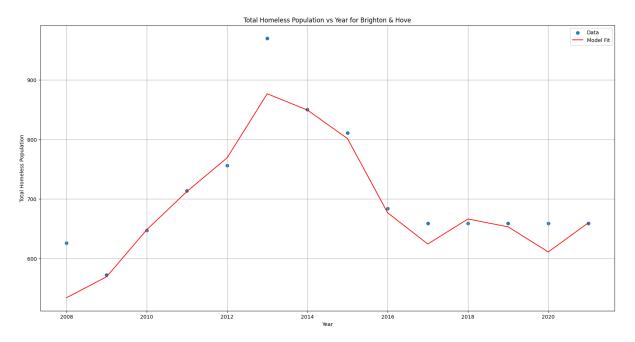


Figure 8: Line of best fit to Brighton & Hove's homeless data as predicted by multiple linear regression model on housing data.

To forecast future changes in homelessness, we plan to develop individual time-series models for each of the various factors. Since each of these individual models can be combined to produce an overall result for homelessness as shown in Equation 7, our resulting model is very flexible and dynamic.

$$U'_{b}h(t) = P'_{b}h(t) + T'_{b}h(t) + A'_{m}(t) + I'_{m}(t) + H'_{d}(t) + \epsilon$$
(7)

5.6 Discussion

The model predicts that housing disparity, as defined in Q2, and median income are the main factors that affect a region's homeless population. A significant disparity between a region's housing availability and its total population, coupled with a low median income, creates a breeding ground for a larger homeless population. When the number of available dwellings falls short of the city's total residents, competition for housing intensifies. This, in turn, drives up housing costs, making it increasingly difficult, especially for low-wage earners, to afford rent or mortgage payments. As a result, individuals and families who fall behind on payments or face unexpected financial hardships are more likely to be evicted or forced to live in doubled-up situations, further straining available resources. This lack of affordable housing options, combined with a low median income that makes saving for emergencies challenging, pushes vulnerable individuals and families towards homelessness.

The model also predicts that the total population of a region and the homeless population of the region are correlated. As the population of a city rises, its homeless population will also naturally rise as the housing disparity increases.

City legislators who want to develop a long-term plan to address homelessness must, over all else, increase the amount of available housing to combat homelessness. The housing disparity can be decreased in two ways: by reducing the population of the city and by increasing the number of available housing units. However, decreasing the population of a city can prove detrimental to the welfare of the city due to decreases in gross domestic product and thus the economic well-being of the city. By increasing the number of available housing units, however, legislators can also drive down the cost of housing, which addresses another key cause of homelessness, a lack of real estate purchasing power.

There are many outside shocks that could potentially disrupt an ideal situation and drive up homelessness. These can be accounted for in our model with variables such as median income and total housing units, whose downturn in a natural disaster or economic recession would affect homelessness in the region.

5.7 Strengths and Weaknesses

Since each of these individual models is combined together to produce an overall result for homelessness, our resulting model is very flexible and dynamic. With more data, we can easily tune and extend this model with additional factors that we find with more research.

However, the most significant weakness of this model is that it cannot fit well onto nonlinear input features as derived from its various sub-models. However, this weakness can be compensated by the fact that the sub-models themselves can be nonlinear.

6 Conclusion

For the first question, we used linear regression to find the total number of housing units available multiple decades into the future. Our model predicted 137,400 units in 2031, 143,400 units in 2041, and 161,500 units in 2071 in Brighton & Hove, and 254,800 units in 2031, 274,100 units in 2041, and 332,100 units in 2071 in Manchester. We used sinusoidal regression with trends to model the homelessness in the two regions over 50 years, finding 0.63% homelessness in 2032, 0.56% homelessness in 2042, and 0.47% homelessness in 2072 in Brighton & Hove, and 0.63% homelessness in 2032, 1.81% homelessness in 2042, and 3.04% homelessness in 2072 in Manchester. Finally, we used a

multivariate linear regression model to examine the effects of 9 variables on homelessness in Brighton & Hove, allowing us to determine that the disparity in housing units available and total population in the region and the median income of the region had the greatest impact on the homeless population of the region.

References

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A Appendix

A.1 Python Code for Question 1

```
# %%
1
  import pandas as pd
2
  import numpy as np
3
  import matplotlib.pyplot as plt
4
  import seaborn as sns
\mathbf{5}
  import os
6
  import statsmodels.api as sm
7
8
  # Load the data
9
  # Go one folder back
10
  os.chdir("..")
11
  path =
12
   bh_housing = pd.read_csv(path)
13
14
  # Convert the Year column to datetime
15
  bh_housing['Year'] = pd.to_datetime(bh_housing['Year'], format='%Y')
16
17
  # Convert all other columns to numeric.
18
  for col in bh_housing.columns[1:]:
19
      if bh_housing[col].dtype == 'object':
20
         # Remove commas and convert to numeric
21
         bh_housing[col] = pd.to_numeric(bh_housing[col].str.replace(',',
22
          23
  print(bh_housing.head())
24
25
  # %%
26
  path =
27
   manchester_housing = pd.read_csv(path)
28
29
  # Convert the Year column to datetime
30
  manchester_housing['Year'] = pd.to_datetime(manchester_housing['Year'],
31
      format='%Y')
    \rightarrow
```

```
32
   # Convert all other columns to numeric.
33
   for col in manchester_housing.columns[1:]:
34
       if manchester_housing[col].dtype == 'object':
35
           # Remove commas and convert to numeric
36
           manchester_housing[col] =
37
            → pd.to_numeric(manchester_housing[col].str.replace(',', ''))
   print(manchester_housing.head())
38
39
   # %%
40
   plt.figure(figsize=(20, 10))
41
   plt.plot(manchester_housing['Year'], manchester_housing['Total housing
42
   → units'], '-o', label='Manchester')
   plt.plot(manchester_housing['Year'], bh_housing['Total housing units'],
43
   → '-o', label='Brighton & Hove')
   plt.xlabel('Year')
44
   plt.ylabel('Total Units')
45
   plt.grid()
46
   plt.legend(loc='upper left')
47
   plt.title('Total Housing Units in Brighton & Hove and Manchester')
48
   plt.show()
49
50
   # %%
51
   # Plot the data for the two cities
52
   plt.figure(figsize=(20, 10))
53
54
   # Make a linear regression using numpy.
55
   m_bh, b_bh = np.polyfit(bh_housing['Year'].dt.year, bh_housing['Total
56
   \rightarrow housing units'], 1)
   print('Brighton & Hove', 'm:', m_bh, 'b:', b_bh)
57
58
   # Calculate the r^2 value
59
   r_squared = np.corrcoef(bh_housing['Year'].dt.year, bh_housing['Total
60
   \rightarrow housing units'])[0, 1]**2
   print(f"R^2: {r_squared}")
61
62
   plt.plot(bh_housing['Year'].dt.year, bh_housing['Total housing units'],
63
      'o', label='Brighton & Hove', color='blue')
   \hookrightarrow
```

```
plt.plot(bh_housing['Year'].dt.year, m_bh*bh_housing['Year'].dt.year +
64
      b_bh, '--', label='Linear Regression Brighton & Hove', color='blue')
   \hookrightarrow
65
   # Make a linear regression using numpy.
66
   m_manchester, b_manchester =
67
       np.polyfit(manchester_housing['Year'].dt.year,
   \hookrightarrow
      manchester_housing['Total housing units'], 1)
   \hookrightarrow
   print('Manchester', 'm:', m_manchester, 'b:', b_manchester)
68
69
   # Calculate the r^2 value
70
   r_squared = np.corrcoef(manchester_housing['Year'].dt.year,
71
   → manchester_housing['Total housing units'])[0, 1]**2
   print(f"R^2: {r_squared}")
72
73
   plt.plot(manchester_housing['Year'].dt.year, manchester_housing['Total
74
   → housing units'], 'o', label='Manchester', color='orange')
   plt.plot(bh_housing['Year'].dt.year,
75
   → m_manchester*bh_housing['Year'].dt.year + b_manchester, '--',
      label='Linear Regression Manchester', color='orange')
   \hookrightarrow
76
   plt.xlabel('Year')
77
   plt.ylabel('Total Housing Units')
78
   plt.grid()
79
   plt.legend(loc='upper left')
80
   plt.title('Total Housing Units in Brighton & Hove and Manchester')
81
   plt.show()
82
83
   # %%
84
   # Create statsmodels linear regression for Brighton & Hove
85
   # Use statsmodels to calculate the confidence interval.
86
   alpha = 0.05 # 95% confidence interval
87
   bh_lr = sm.OLS(bh_housing['Total housing units'],
88
   → sm.add_constant(bh_housing['Year'].dt.year)).fit()
   print('Brighton & Hove')
89
   print(bh_lr.summary())
90
91
   # Create statsmodels linear regression for Manchester
92
   # Use statsmodels to calculate the confidence interval.
93
   alpha = 0.05 # 95% confidence interval
94
```

```
manchester_lr = sm.OLS(manchester_housing['Total housing units'],
95
      sm.add_constant(manchester_housing['Year'].dt.year)).fit()
    \hookrightarrow
   print('\n\n\nManchester')
96
   print(manchester_lr.summary())
97
98
   # Extrapoloate the data for the next 10, 20, 50 years.
99
   # Create confidence intervals for the next 10, 20, 50 years.
100
   years = np.array([2031, 2041, 2071])
101
   bh_conf_interval =
102
    → bh_lr.get_prediction(sm.add_constant(years)).conf_int(alpha=alpha)
   bh_housing_pred_low = bh_conf_interval[:, 0]
103
   bh_housing_pred_average = bh_lr.predict(sm.add_constant(years))
104
   bh_housing_pred_high = bh_conf_interval[:, 1]
105
   print('Brighton & Hove')
106
   for year, pred_low, pred_avg, pred_high in zip(years,
107
    bh_housing_pred_low, bh_housing_pred_average, bh_housing_pred_high):
       print(year, pred_low, pred_high)
108
109
   # Make a table for Brighton & Hove
110
   pred_bh = pd.DataFrame({'Year': years, 'Low': bh_housing_pred_low,
111
    → 'Average': bh_housing_pred_average, 'High': bh_housing_pred_high})
   print(pred_bh)
112
113
   manchester_conf_interval =
114
       manchester_lr.get_prediction(sm.add_constant(years)).conf_int(alpha=alpha)
   manchester_housing_pred_low = manchester_conf_interval[:, 0]
115
   manchester_housing_pred_average =
116
    → manchester_lr.predict(sm.add_constant(years))
   manchester_housing_pred_high = manchester_conf_interval[:, 1]
117
   print('\nManchester')
118
   for year, pred_low, pred_avg, pred_high in zip(years,
119
    → manchester_housing_pred_low, manchester_housing_pred_average,
    \rightarrow manchester_housing_pred_high):
       print(year, pred_low, pred_avg, pred_high)
120
121
   # Make a table for Manchester
122
```

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```
pred_manchester = pd.DataFrame({'Year': years, 'Low':
123
        manchester_housing_pred_low, 'Average':
    \rightarrow
       manchester_housing_pred_average, 'High':
    \hookrightarrow
      manchester_housing_pred_high})
    \hookrightarrow
   print(pred_manchester)
124
125
    # Plot the predicted data for the two cities.
126
   time = np.arange(2022, 2071, 1)
127
   plt.figure(figsize=(20, 10))
128
   plt.plot(time, m_bh*time + b_bh, '--', label='Linear Regression Brighton
129
    → & Hove', color='blue')
   plt fill_between(years, bh_housing_pred_low, bh_housing_pred_high,
130
    \rightarrow color='blue', alpha=0.2)
   plt.plot(time, m_manchester*time + b_manchester, '--', label='Linear
131
    → Regression Manchester', color='orange')
   plt.fill_between(years, manchester_housing_pred_low,
132
    → manchester_housing_pred_high, color='orange', alpha=0.2)
   plt.xlabel('Year')
133
   plt.ylabel('Total Housing Units')
134
   plt.grid()
135
   plt.legend(loc='upper left')
136
   plt.title('Total Housing Units in Brighton & Hove and Manchester')
137
   plt.show()
138
139
    # %%
140
    import pmdarima as pm
141
   from sklearn.model_selection import train_test_split
142
143
   train_x, test_x, train_y, test_y = train_test_split(bh_housing['Year'],
144
       bh_housing['Total housing units'], test_size=0.2, shuffle=False)
145
    # Fit your model
146
   model = pm.auto_arima(train_y, seasonal=True, m=12)
147
148
   forecasts = model.predict(test_y.shape[0]) # predict N steps into the
149
       future
    \hookrightarrow
150
    # Visualize the forecasts (blue=train, green=forecasts)
151
   plt.figure(figsize=(20, 10))
152
```

```
plt.plot(train_x, train_y, c='blue')
153
   plt.plot(test_x, test_y, c='green')
154
   plt.plot(test_x, forecasts, '--', c='green')
155
   plt.legend(['Train', 'Test', 'Forecasts'], loc='upper left')
156
   plt.grid()
157
   plt.title('ARIMA Model for Brighton & Hove')
158
   plt.xlabel('Year')
159
   plt.ylabel('Total Housing Units')
160
   plt.show()
161
162
163
    # %%
164
   train_x, test_x, train_y, test_y =
165
        train_test_split(manchester_housing['Year'],
    \hookrightarrow
        manchester_housing['Total housing units'], test_size=0.2,
        shuffle=False)
    \rightarrow
166
    # Fit your model
167
   model = pm.auto_arima(train_y, seasonal=False)
168
169
    # make your forecasts
170
   forecasts = model.predict(test_y.shape[0]) # predict N steps into the
171
      future
    \hookrightarrow
172
    # Visualize the forecasts (blue=train, green=forecasts)
173
   plt.figure(figsize=(20, 10))
174
   plt.plot(train_x, train_y, c='blue')
175
   plt.plot(test_x, test_y, c='green')
176
   plt.plot(test_x, forecasts, '--', c='green')
177
   plt.legend(['Train', 'Test', 'Forecasts'], loc='upper left')
178
   plt.grid()
179
   plt.title('ARIMA Model for Manchester')
180
   plt.xlabel('Year')
181
   plt.ylabel('Total Housing Units')
182
   plt.show()
183
184
    # %%
185
   # Perform sensitvity analysis for the linear regression model
186
   # For a small change in the model, how much does the output change?
187
```

```
# Check for Brighton & Hove.
188
   m_bh, b_bh = np.polyfit(bh_housing['Year'].dt.year, bh_housing['Total
189
    \rightarrow housing units'], 1)
   default_pred = m_bh*years + b_bh
190
   years = np.array([2031, 2041, 2071])
191
   m = np.linspace(0.95*m_bh, 1.05*m_bh, 5)
192
   b = np.linspace(0.95*b_bh, 1.05*b_bh, 5)
193
194
   # Create a dataframe to store the results
195
   sensitivity_bh_2031 = pd.DataFrame()
196
   sensitivity_bh_2041 = pd.DataFrame()
197
   sensitivity_bh_2071 = pd.DataFrame()
198
   # Make the index the m and the columsn the b.
199
   sensitivity_bh_2031.index = m
200
   sensitivity_bh_2041.index = m
201
   sensitivity_bh_2071.index = m
202
203
    # Loop through the m and b values and calculate the predictions.
204
   for b_val in b:
205
        sensitivity_bh_2031[b_val] = m*2031 + b_val
206
        sensitivity_bh_2041[b_val] = m*2041 + b_val
207
        sensitivity_bh_2071[b_val] = m*2071 + b_val
208
209
        # Calculate the percent difference from the default prediction.
210
        sensitivity_bh_2031[b_val] = (sensitivity_bh_2031[b_val] -
211
        \rightarrow default_pred[0])/default_pred[0]*100
        sensitivity_bh_2041[b_val] = (sensitivity_bh_2041[b_val] -
212
        \rightarrow default_pred[1])/default_pred[1]*100
        sensitivity_bh_2071[b_val] = (sensitivity_bh_2071[b_val] -
213
            default_pred[2])/default_pred[2]*100
214
   # Save the results to a csv file.
215
   sensitivity_bh_2031.to_csv('sensitivity_bh_2031.csv')
216
   sensitivity_bh_2041.to_csv('sensitivity_bh_2041.csv')
217
   sensitivity_bh_2071.to_csv('sensitivity_bh_2071.csv')
218
   print(sensitivity_bh_2031)
219
220
   # Check for Manchester
221
```

```
m_manchester, b_manchester =
222
       np.polyfit(manchester_housing['Year'].dt.year,
    \hookrightarrow
        manchester_housing['Total housing units'], 1)
   default_pred = m_manchester*years + b_manchester
223
   years = np.array([2031, 2041, 2071])
224
   m = np.linspace(0.95*m_manchester, 1.05*m_manchester, 5)
225
   b = np.linspace(0.95*b_manchester, 1.05*b_manchester, 5)
226
227
   # Create a dataframe to store the results
228
   sensitivity_manchester_2031 = pd.DataFrame()
229
   sensitivity_manchester_2041 = pd.DataFrame()
230
   sensitivity_manchester_2071 = pd.DataFrame()
231
232
   # Make the index the m and the columsn the b.
233
   sensitivity_manchester_2031.index = m
234
   sensitivity_manchester_2041.index = m
235
   sensitivity_manchester_2071.index = m
236
237
    # Loop through the m and b values and calculate the predictions.
238
   for b_val in b:
239
        sensitivity_manchester_2031[b_val] = m*2031 + b_val
240
        sensitivity_manchester_2041[b_val] = m*2041 + b_val
241
        sensitivity_manchester_2071[b_val] = m*2071 + b_val
242
243
        # Calculate the percent difference from the default prediction.
244
        sensitivity_manchester_2031[b_val] =
245
            (sensitivity_manchester_2031[b_val]
        \hookrightarrow
            default_pred[0])/default_pred[0]*100
        \hookrightarrow
        sensitivity_manchester_2041[b_val] =
246
            (sensitivity_manchester_2041[b_val] -
         \hookrightarrow
            default_pred[1])/default_pred[1]*100
        sensitivity_manchester_2071[b_val] =
247
            (sensitivity_manchester_2071[b_val] -
            default_pred[2])/default_pred[2]*100
248
   # Save the results to a csv file.
249
   sensitivity_manchester_2031.to_csv('sensitivity_manchester_2031.csv')
250
   sensitivity_manchester_2041.to_csv('sensitivity_manchester_2041.csv')
251
   sensitivity_manchester_2071.to_csv('sensitivity_manchester_2071.csv')
252
```

```
253
254 print(sensitivity_manchester_2031)
255
256
```

A.2 Python Code for Question 2

```
# %%
1
  import pandas as pd
2
  import numpy as np
3
  import matplotlib.pyplot as plt
4
  import seaborn as sns
\mathbf{5}
  import os
6
  import statsmodels.api as sm
\overline{7}
8
  # Load the data
9
  # Go one folder back
10
  os.chdir("..")
11
12
  bh_path =
13
   bh_hl = pd.read_csv(bh_path)
14
15
   # Convert the Year column to datetime
16
  bh_hl['Year'] = pd.to_datetime(bh_hl['Year'], format='%Y')
17
18
   # Convert all other columns to numeric.
19
  for col in bh_hl.columns[1:]:
20
       if bh_hl[col].dtype == 'object':
21
           # If data contains '-', use linear interpolation to fill
22
           \leftrightarrow missing values.
           if ' -' in bh_hl[col].unique():
^{23}
              bh_hl[col] = bh_hl[col].replace(' -', np.nan)
24
25
           # Remove commas and convert to numeric
26
           bh_hl[col] = pd.to_numeric(bh_hl[col].str.replace(',', ''))
27
28
          bh_hl[col] = bh_hl[col].interpolate(method='linear')
29
30
```

```
print(bh_hl)
31
32
33
  hl_path =
34
   manchester_hl = pd.read_csv(hl_path)
35
36
   # Convert the Year column to datetime
37
  manchester_hl['Year'] = pd.to_datetime(manchester_hl['Year'],
38
      format='%Y')
39
   # Convert all other columns to numeric.
40
  for col in manchester_hl.columns[1:]:
41
       if manchester_hl[col].dtype == 'object':
42
           # If data contains '-', use linear interpolation to fill
43
           \rightarrow missing values.
           if ' -' in manchester_hl[col].unique():
44
               manchester_hl[col] = manchester_hl[col].replace(' -',
45
               \rightarrow np.nan)
46
           # Remove commas and convert to numeric
47
           manchester_hl[col] =
48
           → pd.to_numeric(manchester_hl[col].str.replace(',', ''))
49
           manchester_hl[col] =
50
              manchester_hl[col].interpolate(method='linear')
51
  print(manchester_hl)
52
53
   # %%
54
  bh_hl['total homeless'] = bh_hl['Homeless with priority need'] +
55
   → bh_hl['Homeless without priority need']
  bh_hl['homeless percent'] = bh_hl['total homeless'] / bh_hl['Total
56
      number of households']
   \hookrightarrow
57
  manchester_hl['total homeless'] = manchester_hl['Homeless with priority
58
     need'] + manchester_hl['Homeless without priority need']
  manchester_hl['homeless percent'] = manchester_hl['total homeless'] /
59
      manchester_hl['Total number of households']
```

```
60
   # Plot the homeless percent
61
   plt.figure(figsize=(10, 6))
62
   plt.plot(bh_hl['Year'], bh_hl['homeless percent'], label='Brighton &
63
   \rightarrow Hove')
   plt.plot(manchester_hl['Year'], manchester_hl['homeless percent'],
64
   → label='Manchester')
   plt.xlabel('Year')
65
   plt.ylabel('Homeless Percent')
66
   plt.title('Homeless Percent in Brighton & Hove and Manchester')
67
   plt.grid()
68
   plt.legend()
69
   plt.show()
70
71
72
   # %%
73
   # Fit Manchester data to a sine and logistic function
74
   def sine(x, a, b, c, d):
75
       return a * np.sin(b * x + c) + d
76
77
   def logistic(x, a, b, c, d):
78
       return a / (1 + np.exp(-b * (x - c))) + d
79
80
   def line(x, a, b):
81
       return a * x + b
82
83
   def logistic_sine(x, a, b, c, d, e, f, g):
84
       return a / (1 + np.exp(-b * (x - c))) + d + e * np.sin(f * x + g)
85
86
   def line_sine(x, a, b, c, d, e, f):
87
       return a * x + b + c * np.sin(d * x + e) + f
88
89
   # %%
90
   from scipy.optimize import curve_fit
91
   from scipy.stats.distributions import t
92
93
   popt1, pcov1 = curve_fit(sine, bh_hl['Year'].dt.year, bh_hl['homeless
94
   → percent'], p0=[0.1, 0.1, 0.1, 0.1])
95
```

```
# Fit the logistic function
96
   plt.figure(figsize=(10, 6))
97
   plt.plot(bh_hl['Year'].dt.year, bh_hl['homeless percent'],
98
    → label='Brighton & Hove')
   plt.plot(bh_hl['Year'].dt.year, sine(bh_hl['Year'].dt.year, *popt1),
99
    → label='Sine Fit')
   plt.xlabel('Year')
100
   plt.ylabel('Homeless Percent')
101
   plt.title('Homeless Percent in Brighton & Hove')
102
   plt.grid()
103
   plt.legend()
104
   plt.show()
105
106
   # %%
107
   # Predict for the next 50 years.
108
   time = np.arange(2008, 2072, 1)
109
   pred = sine(time, *popt1)
110
111
   plt.figure(figsize=(20, 10))
112
   plt.plot(bh_hl['Year'].dt.year, bh_hl['homeless percent'],
113
    → label='Brighton & Hove')
   plt.plot(time, pred)
114
   plt.xlabel('Year')
115
   plt.ylabel('Homeless Percent')
116
   plt.title('Homeless Percent in Brighton & Hove')
117
   plt.grid()
118
   plt.legend(['Actual', 'Predicted'], loc='upper left')
119
   plt.axvline(x=2031, color='r', linestyle='--')
120
   plt.axvline(x=2041, color='r', linestyle='--')
121
   plt.axvline(x=2071, color='r', linestyle='--')
122
123
   dof = np.size(bh_hl['Year'].dt.year) - 1 # degrees of freedom:
124
   # calculate student-t value
125
   a = 0.05 \# (1-0.95, 95\% CI)
126
   tval = t.ppf(1.0-a/2, dof)
127
128
   ci = tval*np.sqrt(pcov1)
129
   for i in range(len(popt1)):
130
        print("p{0}: {1} +/- {2}".format(i, popt1[i], ci[i, i]))
131
```

```
132
   print('\n2031', pred[2031 - 2008]*100)
133
   print('2041', pred[2041 - 2008]*100)
134
   print('2071', pred[2071 - 2008]*100)
135
136
   plt.show()
137
138
    # %%
139
    # Fit the data to logistic_sine using scipy
140
141
   popt2, pcov2 = curve_fit(logistic_sine, manchester_hl['Year'].dt.year,
142
        manchester_hl['homeless percent'],
                                p0=[0.1, 0.5, 2000, 40, 0.1, 1, 1])
143
144
   popt3, pcov3 = curve_fit(line_sine, manchester_hl['Year'].dt.year,
145
        manchester_hl['homeless percent'],
                                p0=[0.1, 0.5, 4000, 30, 0.1, 1])
146
147
    # Plot the data and the fitted curve
148
   plt.figure(figsize=(10, 6))
149
   plt.plot(manchester_hl['Year'].dt.year, manchester_hl['homeless
150
    → percent'], label='Manchester')
    # plt.plot(manchester_hl['Year'],
151
       logistic_sine(manchester_hl['Year'].dt.year, *popt),
    \hookrightarrow
       label='Logistic Sine Fit')
     \rightarrow 
   plt.plot(manchester_hl['Year'].dt.year,
152
       line_sine(manchester_hl['Year'].dt.year, *popt3), label='Logistic
    \hookrightarrow
      Fit')
    \hookrightarrow
   plt.xlabel('Year')
153
   plt.ylabel('Homeless Percent')
154
   plt.title('Homeless Percent in Manchester')
155
   plt.grid()
156
   plt.legend()
157
   plt.show()
158
159
    # %%
160
    # Predict for the next 50 years.
161
   time = np.arange(2008, 2072, 1)
162
   pred = line_sine(time, *popt3)
163
```

```
164
   plt.figure(figsize=(20, 10))
165
   plt.plot(manchester_hl['Year'].dt.year, manchester_hl['homeless
166
    → percent'], label='Manchester')
   plt.plot(time, pred)
167
   plt.xlabel('Year')
168
   plt.ylabel('Homeless Percent')
169
   plt.title('Predicted Homeless Percent in Manchester')
170
   plt.grid()
171
   plt.legend(['Actual', 'Predicted'], loc='upper left')
172
   plt.axvline(x=2031, color='r', linestyle='--')
173
   plt.axvline(x=2041, color='r', linestyle='--')
174
   plt.axvline(x=2071, color='r', linestyle='--')
175
176
   print('2031', pred[2031 - 2008]*100)
177
   print('2041', pred[2041 - 2008]*100)
178
   print('2071', pred[2071 - 2008]*100)
179
180
   plt.show()
181
182
   # %%
183
   from statsmodels.tsa.stattools import adfuller
184
   test_result=adfuller(manchester_hl['homeless percent'])
185
   test_result
186
187
   # %%
188
   manchester_hl['Seasonal first difference'] = manchester_hl['total
189
    → homeless'] - manchester_hl['total homeless'].shift(6)
   manchester_hl.head(14)
190
191
   # %%
192
   adfuller(manchester_hl['Seasonal first difference'].dropna())
193
194
   # %%
195
   from statsmodels.tsa.seasonal import seasonal_decompose
196
   result = seasonal_decompose(manchester_hl['Year'])
197
   result.plot()
198
199
   # %%
200
```

```
from sklearn.svm import SVR
201
   from sklearn.pipeline import make_pipeline
202
   from sklearn.model_selection import train_test_split
203
   from sklearn.preprocessing import StandardScaler
204
205
   X_train, X_test, y_train, y_test =
206
       train_test_split(manchester_hl['Year'], manchester_hl['homeless
       percent'], train_size=0.8, test_size=0.2, shuffle=False)
207
   X_train, X_test, y_train, y_test = X_train.to_frame(),
208
       X_test to_frame(), y_train to_frame(), y_test to_frame()
209
   regr = make_pipeline(StandardScaler(), SVR(C=0.5, epsilon=5))
210
211
   regr fit(X_train, y_train)
212
   forecasts = regr.predict(X_test)
213
214
   # x = np.arange(X_train + X_test)
215
   plt.plot(X_train, y_train, c='blue')
216
   plt.plot(X_test, y_test, c='red')
217
   plt.plot(X_test, forecasts, c='green')
218
   plt.show()
219
220
   # %%
221
   import pmdarima as pm
222
   from sklearn.model_selection import train_test_split
223
224
   manchester_hl['total homeless'] = manchester_hl['Homeless with priority
225
        need'] + manchester_hl['Homeless without priority need']
226
   manchester_hl['homeless percent'] = manchester_hl['total homeless'] /
227
        manchester_hl['Total number of households']
    \hookrightarrow
228
   X_train, X_test, y_train, y_test =
229
        train_test_split(manchester_hl['Year'], manchester_hl['total
        homeless'], train_size=0.7, shuffle=False)
230
   model = pm.auto_arima(y_train, seasonal=True, m=3, seasonal_test='ch')
231
232
```

```
forecasts = model.predict(X_test.shape[0])
233
234
    # x = np.arange(X_train + X_test)
235
    plt.plot(X_train, y_train, c='blue')
236
    plt.plot(X_test, y_test, c='red')
237
    plt.plot(X_test, forecasts, c='green')
238
    plt.show()
239
240
    # %%
241
242
243
    # %%
244
245
246
247
```

A.3 Python Code for Question 3

```
# %%
1
  # Make a ML model to predict the target variable
2
  import pandas as pd
3
  import numpy as np
4
  import matplotlib.pyplot as plt
\mathbf{5}
  import seaborn as sns
6
  import os
7
8
  # Load the data
9
  # Go one folder back
10
  os.chdir("..")
11
12
  path =
13
   data = pd.read_csv(path)
14
15
  # Convert the Year column to datetime
16
  data['Year'] = pd.to_datetime(data['Year'], format='%Y')
17
18
  # Convert all other columns to numeric.
19
  for col in data.columns[1:]:
20
```

```
if data[col].dtype == 'object':
21
           # If data contains '-', use linear interpolation to fill
22
            \rightarrow missing values.
           if ' -' in data[col].unique():
23
                data[col] = data[col].replace(' -', np.nan)
24
25
           # Remove commas and convert to numeric
26
           data[col] = pd.to_numeric(data[col].str.replace(',', ''))
27
28
           data[col] = data[col].interpolate(method='linear')
29
30
   print(data)
31
32
   # %%
33
   data['Total Homeless'] = data['Homeless, priority need'] +
34
   → data['Homeless, not priority need']
   data['Homeless Percent'] = data['Total Homeless'] / data['Total number
35
   \rightarrow of households']
   data['Housing Disparity'] = data['Total number of households'] -
36
   → data['Total Housing Units']
   # data['Population Change'] = data['Total Population'] - data['Total
37
   \rightarrow Population'].shift(1)
   # data['Homeless Change'] = data['Total Homeless'] - data['Total
38
   \rightarrow Homeless'].shift(1)
39
   data.drop(['Homeless, priority need', 'Homeless, not priority need',
40
      'Eligible but not homeless'], axis=1, inplace=True)
41
   # Make a correlation matrix
42
   correlation_matrix = data.corr()
43
   sns.heatmap(correlation_matrix, annot=True)
44
   plt.title('Correlation Heat Map')
45
   # data.drop(['Homeless Percent'], axis=1, inplace=True)
46
   plt.show()
47
48
   data_copy = data.copy()
49
50
   # %%
51
   from sklearn.model_selection import train_test_split
52
```

```
53
   # Convert the Year column to numeric
54
   data['Year'] = data['Year'].dt.year
55
56
   # Split the data into training and testing sets
57
   # Drop other variable
58
   data.fillna(0, inplace=True)
59
60
   data.drop(['Homeless Percent'], axis=1, inplace=True)
61
62
63
   X = data.drop(['Total Homeless'], axis=1)
64
   y = data['Total Homeless']
65
66
   X_train, X_test, y_train, y_test = train_test_split(X, y, test_size=0.3,
67
       random_state=42)
   \hookrightarrow
68
   from sklearn.linear_model import LinearRegression
69
   from sklearn.metrics import mean_squared_error
70
71
   # Train the model
72
   model = LinearRegression()
73
   model fit(X_train, y_train)
74
75
   # Make predictions
76
   y_pred = model.predict(X_test)
77
78
   # Calculate the mean squared error
79
   mse = mean_squared_error(y_test, y_pred)
80
   print('Mean Squared Error:', mse)
81
82
   # R^2 score
83
   r2 = model.score(X, y)
84
   print('R^2:', r2)
85
86
   # Print the coefficients
87
   print('Coefficients:', model.coef_)
88
89
   # Plot the fit.
90
```

```
# X = np.linspace(data['Year'].min(), data['Year'].max() + 50, 1)
91
   pred = model.predict(X)
92
   plt.figure(figsize=(20, 10))
93
   plt.scatter(data['Year'], data['Total Homeless'])
94
   plt.plot(data['Year'], pred, color='red')
95
   plt.title('Total Homeless Population vs Year for Brighton & Hove')
96
   plt.xlabel('Year')
97
   plt.ylabel('Total Homeless Population')
98
   plt.legend(['Data', 'Model Fit'])
99
   plt.grid()
100
   plt.show()
101
102
    # %%
103
    # Make models for Total number of households, Total Population, Total
104
    \rightarrow Housing Units, and Median Income
    total_households = data['Total number of households']
105
   total_population = data['Total Population']
106
   total_housing_units = data['Total Housing Units']
107
   median_income = data['Median Income']
108
109
    # Plot over time.
110
   plt.plot(data['Year'], total_population)
111
   plt.title('Total number of households vs Year')
112
   plt.xlabel('Year')
113
   plt.ylabel('Total number of households')
114
   plt.show()
115
116
    # %%
117
    # Train a model
118
   from pycaret.time_series import TSForecastingExperiment
119
   s = TSForecastingExperiment()
120
121
   s.setup(data=data_copy, session_id=42, target='Homeless Percent',
122
        numeric_imputation_target='mean',
    \hookrightarrow
        numeric_imputation_exogenous='mean')
123
   best = s.compare_models()
124
125
   # %%
126
```

127 # OOP API
128 s.plot_model(best, plot = 'forecast', data_kwargs = {'fh' : 50})
129
130